

WHAT IS CLAIMED IS:

1. A method for identification, comprising the steps of:

(a) generating system parameters  $G_1$ ,  $G_2$ ,  $P$  and  $\hat{e}$  and storing the system parameters in a memory by a system administrator, wherein  $G_1$  and  $G_2$  are cyclic groups of order  $m$ ,  $P$  is a generator on the cyclic group  $G_1$ ,  $\hat{e}$  is a bilinear map defined as

$$\hat{e}: G_1 \times G_1 \mapsto G_2;$$

(b) generating a private key  $\langle a, b, c \rangle$  and a public key  $v$  and storing the public key  $v$  in the memory by a prover or the system administrator, wherein  $a$ ,  $b$  and  $c$  are randomly chosen in  $Z_m^*$  where  $Z_m^*$  is a multiplicative group of order  $m$ ;

(c) generating random numbers  $r_1, r_2, r_3 \in Z_m^*$  for obtaining an evidence  $(x, Q)$  and sending the evidence  $(x, Q)$  to a verifier by the prover;

(d) receiving the evidence  $(x, Q)$ , selecting a randomly selected number  $\omega \in Z_m^*$  to obtain a query  $R$ , storing the evidence  $(x, Q)$  and the randomly selected number  $\omega$  in the memory and sending the query  $R$  to the prover by the verifier;

(e) receiving the query  $R$ , computing a temporary value  $S$  to obtain a response  $Y$  and sending the response  $Y$  to the verifier by the prover; and

(f) determining a legitimacy of the prover by employing the system parameters  $G_1$ ,  $G_2$ ,  $P$  and  $\hat{e}$ , the public key  $v$ , the evidence  $(x, Q)$  and the randomly selected number  $\omega$  by the verifier.

2. The method of claim 1, wherein, in the step (b), the public key  $v$  is obtained by

$$v = \hat{e}(P, P)^{abc}$$

3. The method of claim 2, wherein, in the step (c), the evidence  $(x, Q)$  includes a

$$x = \hat{e}(P, P)^{r_1 r_2 r_3}$$

first evidence value and a second evidence value

$$Q = r_1 r_2 r_3 P$$

4. The method of claim 3, wherein, in the step (d), the query  $R$  is obtained by

$$R = \omega P$$

5. The method of claim 4, wherein, in the step (e), the temporary value  $S$  is obtained

$$S = r_1 r_2 r_3 R$$

by and the response  $Y$  is obtained by

$$Y = abcP + (a + b + c)S$$

6. The method of claim 5, wherein the verifier determines the legitimacy of the prover by verifying

$$\begin{aligned}
\hat{e}(Y,P) &= \hat{e}(abcP+(a+b+c)S,P) \\
&= \hat{e}(abcP+(a+b+c)r_1r_2r_3R,P) \\
&= \hat{e}(abcP+(a+b+c)r_1r_2r_3^\omega P,P) \\
&= \hat{e}((abc+(a+b+c)r_1r_2r_3^\omega)P,P) \\
&= \hat{e}(P,P)^{abc+(a+b+c)r_1r_2r_3^\omega} \\
&= \hat{e}(P,P)^{abc} \cdot \hat{e}(P,P)^{(a+b+c)r_1r_2r_3^\omega} \\
&= \hat{e}(P,P)^{abc} \cdot \hat{e}(P,r_1r_2r_3P)^{(a+b+c)\omega} \\
&= \hat{e}(P,P)^{abc} \cdot \hat{e}(P,Q)^{(a+b+c)\omega} \\
&= \hat{e}(P,P)^{abc} \cdot \hat{e}((a+b+c),PQ)^\omega \\
&= \hat{e}(P,P)^{abc} \cdot \hat{e}(aP+bP+cP,Q)^\omega \\
&= v \cdot \hat{e}(aP+bP+cP,Q)^\omega
\end{aligned}$$

7. A method for identification, comprising the steps of:

(a) generating system parameters  $G_1$ ,  $G_2$ ,  $P$  and  $\hat{e}$  and storing the system parameters in a memory by a system administrator, wherein  $G_1$  and  $G_2$  are cyclic groups of order  $m$ ,  $P$  is a generator on the cyclic group  $G_1$ ,  $\hat{e}$  is a bilinear map defined as

$$\hat{e}: G_1 \times G_1 \mapsto G_2;$$

(b) generating a private key  $\langle a_1, a_2, \dots, a_n \rangle$  and a public key  $v$  and storing the public key  $v$  in the memory by a prover or the system administrator, wherein  $a_1, a_2, \dots, a_n$  are randomly chosen in  $Z_m^*$  where  $Z_m^*$  is a multiplicative group of order  $m$ ;

(c) generating random numbers  $r_1, r_2, \dots, r_n \in Z_m^*$  for obtaining an evidence  $(x, Q)$  and sending the evidence  $(x, Q)$  to a verifier by the prover;

(d) receiving the evidence  $(x, Q)$ , selecting a randomly selected number  $\omega \in Z_m^*$  to obtain a query  $R$ , storing the evidence  $(x, Q)$  and the randomly selected number  $\omega$  in the memory and sending the query  $R$  to the prover by the verifier;

(e) receiving the query  $R$ , computing a temporary value  $S$  to obtain a response  $Y$  and sending the response  $Y$  to the verifier by the prover; and

(f) determining a legitimacy of the prover by employing the system parameters  $G_1, G_2, P$  and  $\hat{e}$ , the public key  $v$ , the evidence  $(x, Q)$  and the randomly selected number  $\omega$  by the verifier.

8. The method of claim 7, wherein, in the step (b), the public key  $v$  is obtained by  $v = \hat{e}(P, P)^{a_1 a_2 \dots a_n}$ .

9. The method of claim 8, wherein, in the step (c), the evidence  $(x, Q)$  includes a first evidence value  $x = \hat{e}(P, P)^{r_1 r_2 \dots r_n}$  and a second evidence value  $Q = r_1 r_2 \dots r_n P$ .

10. The method of claim 9, wherein, in the step (d), the query  $R$  is obtained by

$$R = \omega P$$

11. The method of claim 10, wherein, in the step (e), the temporary value  $S$  is obtained by  $S = r_1 r_2 \dots r_n R$  and the response  $Y$  is obtained by  $Y = a_1 a_2 \dots a_n P + (a_1 + a_2 + \dots + a_n) S$

12. The method of claim 11, wherein the verifier determines the legitimacy of the prover by verifying

$$\begin{aligned}
 \hat{e}(Y, P) &= \hat{e}(a_1 a_2 \dots a_n P + (a_1 + a_2 + \dots + a_n) S, P) \\
 &= \hat{e}(a_1 a_2 \dots a_n P + (a_1 + a_2 + \dots + a_n) r_1 r_2 \dots r_n R, P) \\
 &= \hat{e}(a_1 a_2 \dots a_n P + (a_1 + a_2 + \dots + a_n) r_1 r_2 \dots r_n \omega P, P) \\
 &= \hat{e}((a_1 a_2 \dots a_n + (a_1 + a_2 + \dots + a_n) r_1 r_2 \dots r_n \omega) P, P) \\
 &= \hat{e}(P, P)^{a_1 a_2 \dots a_n + (a_1 + a_2 + \dots + a_n) r_1 r_2 \dots r_n \omega} \\
 &= \hat{e}(P, P)^{a_1 a_2 \dots a_n} \cdot \hat{e}(P, P)^{(a_1 + a_2 + \dots + a_n) r_1 r_2 \dots r_n \omega} \\
 &= \hat{e}(P, P)^{a_1 a_2 \dots a_n} \cdot \hat{e}(P, r_1 r_2 \dots r_n P)^{(a_1 + a_2 + \dots + a_n) \omega} \\
 &= \hat{e}(P, P)^{a_1 a_2 \dots a_n} \cdot \hat{e}(P, Q)^{(a_1 + a_2 + \dots + a_n) \omega} \\
 &= \hat{e}(P, P)^{a_1 a_2 \dots a_n} \cdot \hat{e}((a_1 + a_2 + \dots + a_n), PQ)^\omega \\
 &= \hat{e}(P, P)^{a_1 a_2 \dots a_n} \cdot \hat{e}(a_1 P + a_2 P + \dots + a_n P, Q)^\omega \\
 &= v \cdot \hat{e}(a_1 P + a_2 P + \dots + a_n P, Q)^\omega.
 \end{aligned}$$